WAY KUO | XIAOYAN ZHU

IMPORTANCE MEASURES IN RELIABILITY, RISK, AND OPTIMIZATION PRINCIPLES AND APPLICATIONS



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