Wavelets in Electromagnetics and Device Modeling

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Arizona State University Tempe, Arizona



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Dedicated to my father Pan Zhen and mother Lei Tian-Lu

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