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# **HANDBOOK OF INDUSTRIAL MIXING SCIENCE AND PRACTICE**

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Edited by

**Edward L. Paul**

Merck & Co., Inc.  
Rahway, New Jersey

**Victor A. Atiemo-Obeng**

The Dow Chemical Company  
Midland, Michigan

**Suzanne M. Kresta**

University of Alberta  
Edmonton, Canada



**Sponsored by the North American Mixing Forum**



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