
VERIFICATION OF SYSTEMS AND CIRCUITS USING LOTOS, PETRI NETS, AND CCS

BY

Michael Yoeli and Rakefet Kol

Technion—Israel Institute of Technology

Haifa, Israel



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Published by John Wiley & Sons, Inc., Hoboken, New Jersey.

Published simultaneously in Canada.

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Library of Congress Cataloging-in-Publication Data:

Yoeli, Michael, 1917-

Verification of systems and circuits using LOTOS, Petri Nets, and CCS / Michael Yoeli & Rakefet Kol.
p. cm. — (Wiley series on parallel and distributed computing)

Includes index.

ISBN 978-0-471-70449-2 (cloth)

1. Integrated circuits—Verification. 2. Computer software—Verification.
 3. LOTOS (Computer program language) 4. Petri nets. I. Kol, Rakefet. II. Title.
- TK7874.58.Y64 2008
621.3815'48—dc22

2007033487

Printed in the United States of America

10 9 8 7 6 5 4 3 2 1

*To my spouse Nehama, with thanks for her persistent and
helpful encouragement.*

Michael

To my family, with endless love.

Rakefet

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