

**Ocean Acoustic Propagation
by Finite Difference Methods**

D. LEE & S. T. McDANIEL

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OCEAN ACOUSTIC PROPAGATION BY FINITE DIFFERENCE METHODS

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OCEAN ACOUSTIC PROPAGATION BY FINITE DIFFERENCE METHODS

by

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