

Introduction to Hypoplasticity

D. Kolymbas

Advances in Geotechnical Engineering and Tunnelling

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INTRODUCTION TO HYPOPLASTICITY

ADVANCES IN GEOTECHNICAL ENGINEERING AND TUNNELLING

1

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Foreword of the Editor

This booklet inaugurates the series *Advances in Geotechnical Engineering and Tunnelling*. Subsequent issues will follow in irregular terms, either in German or in English language.

The present publication aims to give the reader a short, tractable and as far as possible complete introduction to the young theory of hypoplasticity, which is a new approach to constitutive modelling of granular media in terms of rational continuum mechanics.

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